Mathematical Methods for Social Scientists Math 196 (Sec 45), Winter 2006

Revision Sheet for Mid-term 2

This mid-term will cover those sections in the text book which we have studied in class upto 5.3 and will concentrate on the material covered since the first mid-term. The following questions are of the style you can expect in the exam.

- (1) (a) Define what it means for a matrix to be upper triangular, lower triagular or diagonal.
 - (b) If A and B are upper triagular matrices, what can you say about AB and A^{t} ?
 - (c) Write

$$\left(\begin{array}{cc} 2 & 3 \\ -2 & 4 \end{array}\right)$$

as a product of elementary matrices.

- (2) (a) Give three conditions that are equivalent to a matrix A being invertible.
 - (b) Give a formula for the inverse of a matrix A.
 - (c) Calculate the inverse of

$$\left(\begin{array}{ccc}
2 & 6 & 3 \\
-2 & 8 & 4 \\
0 & -2 & 0
\end{array}\right)$$

using this formula.

(d) Compute the determinant of

$$\left(\begin{array}{ccccc}
2 & 3 & 4 & 1 \\
1 & 3 & 2 & 3 \\
0 & 0 & 2 & 4 \\
0 & 0 & 4 & 9
\end{array}\right)$$

- (3) (a) Define a subspace. Show that the set of solutions to a system of homogeneous equations is a subspace.
 - (b) Define the row space and column space of a matrix. Explain why the row spaces of two row equivalent matrices are the same.
 - (c) Define what it means for a set of vectors to be linearly independent.
 - (d) Show that $\{(0,1,1),(1,0,1),(1,1,0)\}$ is linearly independent.
- (4) (a) Define what a basis is for a vector space. Define the dimension of a vector space what fact means this definition is sensible?
 - (b) Give two conditions that are equivalent to being a basis.
 - (c) Is the set $\{(-1,2,1),(2,3,1),(7,7,2)\}$ linearly independent? Justify your answer. Find a basis for the span of this set.

It will be useful to review your homework and make sure you understand it. I will also ask questions from the text book.